

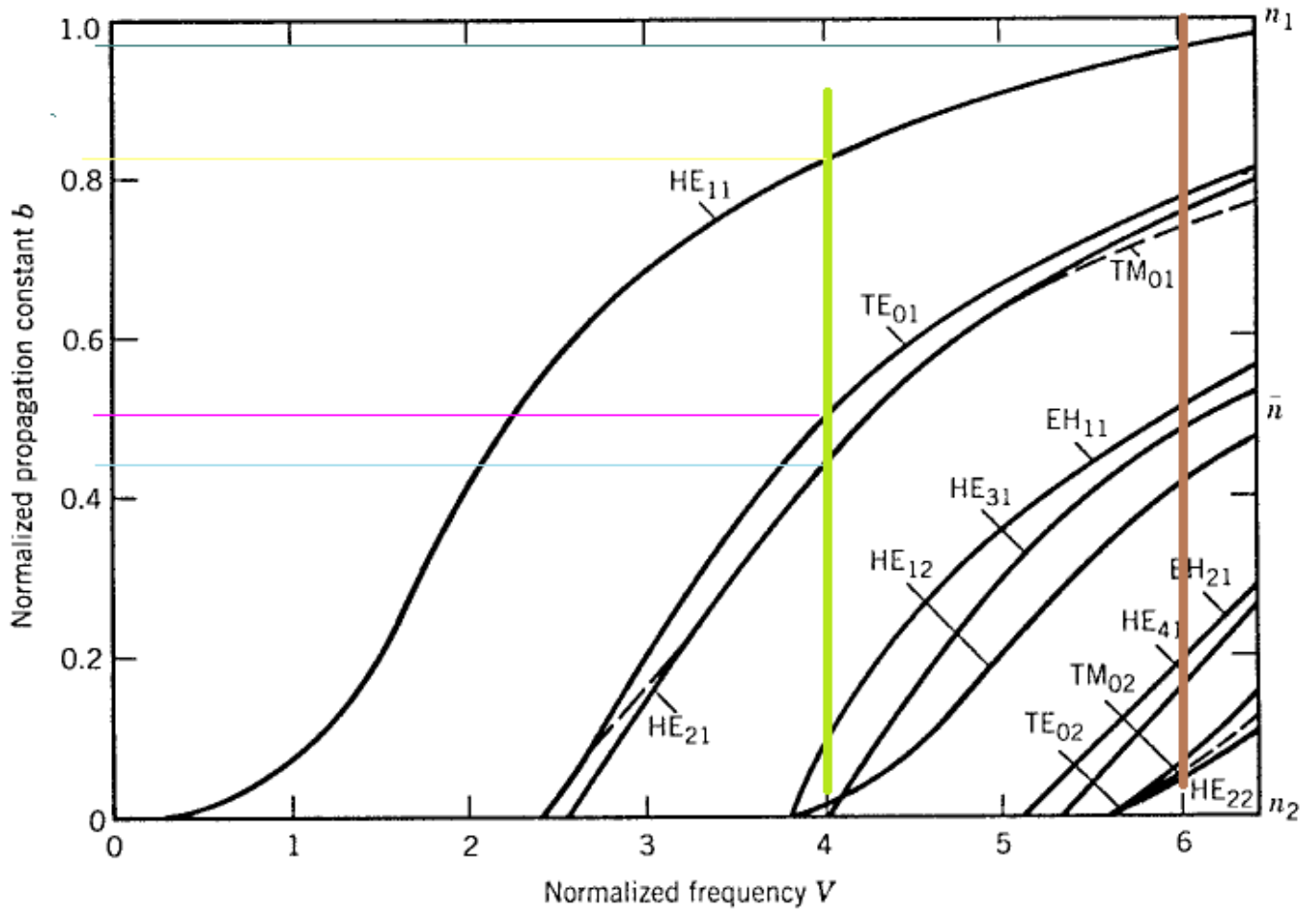
# Çankaya University – ECE Department – ECE 635

2013 Autumn Term

**Experiment 0** : Finding beta and propagating modes of the fibre

**Experiment in MATLAB is on the course webpage [ece635.cankaya.edu.tr](http://ece635.cankaya.edu.tr). File name is “Findingbeta\_Exp0.m”.**

1. Copy the experiment file into the directory of your name.
2. Run the file, observe the OPs, do not record anything yet. Try to follow what is intended and what is happening
3. This experiment is intended to find the propagation constants ( $\beta$ ) and identify the propagating modes in a step index fibre. For this purpose, the characteristic equation (CE) is written for both  $HE_{vm}$  and  $EH_{vm}$  and  $TE_{0m}$  and  $TM_{0m}$  modes. Note that the first (and in case of  $TM_{0m}$  the second as well) lines are in the original form of CE, but they create singularities due to zero crossings of Bessel functions in the denominator. Hence, they are eliminated by multiplying both sides of the equation by the Bessel function of the denominator. These are the forms used to plot both graphs .
4. In the first graph, we see in 3D the plot of CE for the selected modes. This picture helps us identify the zero crossings (zeros,  $m$ ) of CE at selected  $v$  parameter for all modes in question. The second set of graphs (contour plots) display the zero crossing more clearly on a two dimensional plane and are the contour plots of the all CEs with the normalized frequency  $V$  circles added.
5. By incrementing  $v$  in the range 1 to 8 (in integer increments), find the  $HE_{vm}$  and  $EH_{vm}$  modes for  $V$  values up to 10. Identify these modes one by one and their cut-off  $V$  values, i.e. at which minimum value of  $V$  excludes them. Tabulate these results.
6. By the other CE equations (further down) in the programme, find the  $TE_{0m}$  and  $TM_{0m}$  modes for  $V$  alues up to 10. Identify these modes one by one and their cut-off  $V$  values, i.e. at which minimum value of  $V$  excludes them. Tabulate these results in a separate table.
7. Find the propagation constants, and its normalized values i.e.  $\beta$  and  $\beta_n$  s following the steps given in Example 3.1 of “ECE 635\_Notes on Fibre Propagation\_Jan\_2013\_HTE”.
8. Confirm that these propagation constants, i.e.,  $\beta$  s, are in agreement with  $b_n$  values read from the graph on the next page, also following the steps of Example 3.2.
9. Include your comments for the experiment



Sample Calculation : By running the Findingbeta\_Exp0.m at the settings given, we get the following contour plot, i.e. the graph for  $TM_{0m}$ . From there, we take the  $V = 4$  and get the intersection of this circle with the  $TM_{01}$  curve. Now following Example 3.1 and 3.2, and noting the refractive index values of core and the cladding in the given Matlab file, we proceed as follows

$$n_1 = 1.50, n_2 = 1.47, \lambda = 1.55 \mu\text{m}, u_n = \dots, w_n = \dots$$

$$a = \frac{V}{k(n_1^2 - n_2^2)^{0.5}} = \frac{4}{\frac{2\pi}{1.55 \times 10^{-6}} (1.5^2 - 1.47^2)^{0.5}} = 3.3$$

$$\beta_n = (a^2 k_1^2 - u_n^2)^{0.5} = 19.8756 \quad \text{or} \quad \beta_n = (a^2 k_2^2 + w_n^2)^{0.5} = 19.8697, \quad \beta = \frac{\beta_n}{a} = 6.0124 \times 10^6$$

$$k_2 = 5.9589 \times 10^6, \quad k_1 = 6.0805 \times 10^6, \quad k_2 \leq \beta \leq k_1$$

$$\beta = \frac{\beta_n}{a} = 6.0124 \times 10^6$$

$$b_n = \frac{\beta/k - n_2}{n_1 - n_2} \quad \text{inserting } \beta = 6.0124 \times 10^6, \quad n_1 = 1.50, \quad n_2 = 1.47, \quad k = \frac{2\pi}{\lambda} = 4.0537 \times 10^6$$

$$b_n = 0.44$$

The value of  $b_n = 0.44$  seems to agree well with the intersection of  $TM_{01}$  found in the graph of  $b_n$  against  $V$ .